Lesson 16 Traveling Through the Solar System

Approximate time needed for lesson: Two 50-minute class periods or one 90-minute class period

NCTM Standards

- Measurement: Apply appropriate techniques, tools, and formulas to determine measurements
- Data Analysis and Probability: Develop and evaluate inferences and predictions that are based on data
- Algebra: Analyze change in various contexts
- **Connections:** Recognize and apply mathematics in contexts outside of mathematics
- **Problem Solving:** Build new mathematical knowledge through problem solving

Goals for Students

- ▶ To use calculator and non-calculator methods for analyzing data
- ▶ To apply data collection and analysis in a study of mass and weight
- ▶ To enhance and apply the concept of line of best fit

Description or Summary of Lesson

Mappropriate only for those enrolled in Pre-algebra or Algebra I. Using appropriate technology and working in small groups, students collect data by measuring the mass of various objects. Using calculator and non-calculator methods, students will represent and analyze data to determine relationships, make predictions using a line of best fit, and formulate written conclusions. The line of best fit portions of the lesson may be used to introduce the concept of line of best fit and its applications in making predictions.

Background Information

S tudents should have mastered graphing in a plane, be familiar with using a balance scale, have mastered using formulas, and be familiar with basic graphing calculator keys. The portions on line of best fit assume some prior knowledge of the concepts of slope and y-intercept.

Materials and Equipment -

- Overhead projector and calculator and view screen
- Raisins
- Centicubes or other gram weights
- Each pair of students will need
 - access to a graphing calculator
 - handouts

- Balance scale
- ► A few uncooked spaghetti noodles
- Grid paper
- Construction paper
- **Glue**

Lesson 16: Outline

- **I.** Teacher reviews graphing points, slope as change in the dependent variable divided by the change in the independent variable, and y-intercept as the y-coordinate of the point where the line crosses the y-axis.
- **II.** Students measure the mass of different amounts of raisins.
- **III.** Students use Activity 1, Handout 1, to record and graph the results by hand and with the calculator.
- **IV.** Students analyze the data and complete Activity 1, Handout 1, using a graphing calculator and the Calculator Instructions in Activity 1, Handout 2.
- V. Teacher and students agree on the formula: planet weight = Earth weight x the planet's gravitational factor.
- **VI.** The teacher will choose a celebrity and guide all students through an example including using the steps on Activity 2, Handout 2.
- VII. Working in small groups, students perform the same calculations for a second celebrity and record on Activity 2, Handout 1.
- VIII. To complete Activity 2, Handout 1, students find their own weight on all planets and graph the resulting data.

Activity 1. Raisins: Collecting Data to Explore Mass Handout 1: Data Sheet

If using raisins presents a problem, paper clips or other items could be substituted. *Sample Answers:*

1. Find the measures of the following using a balance scale. Place the given number of raisins on one side of the balance. Place centicubes (or other gram weights) on the other side of the balance until both sides are the same. The raisins weigh the number of centicubes. Remember 1 centicube has a mass of 1 gram. Write the results in the table.

| Number of Raisins | Mass in grams |
|-------------------|---------------|
| 10 | 3 |
| 20 | 6 |
| 25 | 8 |
| 30 | 9 |
| 40 | 12 |

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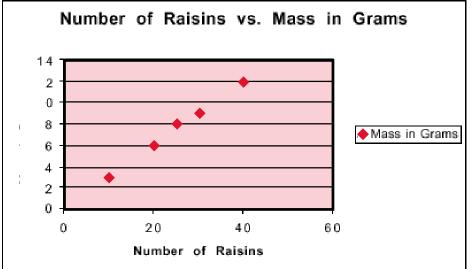
I, Handout

Sample Answers for Activity 1, Handout 1 (continued):

- 2. What is the independent variable? The number of raisins
- 3. What is the dependent variable? The mass in number of grams
- 4. Are these variables related? Yes

If so, how are they related? As the number of raisins increases, the mass in grams increases. For every 10 raisins, the mass goes up about 3 grams.

5. On grid paper, graph the number of raisins vs. the corresponding mass. Choose an appropriate scale.



- 6. What relationship is shown by the data points? A linear or line-like relationship. As the number of raisins (x-values) increases, so do the grams (y-values).
- 7. Is there a positive relationship (that is, does the dependent variable increase/decrease when the independent variable increases/decreases), a negative relationship (that is, does the dependent variable increase/decrease when the independent variable decreases/increases), or no consistent relationship? A positive relationship.
- 8. Even though the data points may not be in exactly one straight line, there may be a line that is close to most, if not all points. This is called **the line of best fit**. Use the spaghetti to find this line of best fit. Does the spaghetti intersect with every point, come close to most points, or not intersect any point? Answers will vary. The spaghetti or line may miss a few of the data points (only misses one in the sample graph in #5) but should be close to most of the points.
- 9. What number value is the slope? To find the slope, choose any two of the data points that fall on or very close to the spaghetti and use the slope formula:

$$= \frac{y_2 - y_1}{x_2 - x_1}$$

m

Example: If the two data points chosen are (10, 3) and (30, 9) and are substituted in the formula for slope, then Slope = $\underline{9-3}$ or 6/20 or 3/10 30-10

Sample Answers for Activity 1, Handout 1 (continued):

- 10. What does the slope represent in this problem? The rate of change of mass in grams to change in number of raisins, or the ratio of grams to raisins. Weight of one raisin.
- 11. According to the data, what should the y-intercept be? **0 since 0 raisins would weigh**

0 grams.

- 12. What is the y-intercept according to the line of best fit (spaghetti)? **0 or close to it.**
- 13. Is the value of #11 different from the value of #12? Why/Why not? Because there is always error in measurement, there may be some difference in the values, but they will be close.
- 14. Write an equation for the line made by the spaghetti in the form y = mx + b where m is the slope and b is the y-intercept. Y = .3x + 0 or just Y = .3x or Y = 3/10 x
- 15. Predict the missing values in the table by using the linear equation you found in #14.

| Number of Raisins | Mass in grams |
|-------------------|---------------|
| 10 | 3 |
| 4 | 1.2 |
| 53.333 | 16 |
| 316.666 | 95 |

- 16. Make a real-life graph. On a piece of heavier paper (construction paper, poster board), create an appropriate title for this graph. Draw axes for the first quadrant. Draw the hash marks along the axes and choose an appropriate scale. Glue the raisin pieces at the data points from #1. Glue on spaghetti as the line of best fit. Label the line of best fit with the equation from #14.
- 17. Use the graphing calculator and the Calculator Instructions in Handout 2 to find the value of the slope (a) and y-intercept (b). (Round to the hundredths place)

Slope = <u>.3</u>

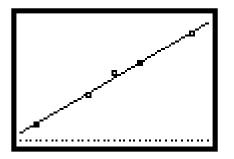
Y-intercept = ___**.1**___

The equation for a line is y = mx + b (m = slope and b = y-intercept)

18. What is the equation of this line? y = x + .1

(*Hint:* use substitution)

19. Sketch the graph of the line from your calculator screen.



Sample Answers for Activity 1, Handout 1 (continued):

20. How does the calculator slope and y-intercept compare with the slope and y-intercept from the spaghetti and pencil-and-paper calculations?

The two graphs, as well and the slope and y-intercept, should be similar.

21. Name three new concepts that you learned from the experiment and/or three things that you now understand better because of the experiment.

Answers will vary. Examples: Learned that slope is a ratio or the rate of change of one variable in terms of the other variable; that slope is positive if the dependent variable increases as the independent variable increases; that the y-intercept is the y-coordinate when the x-coordinate is 0 or that the y-intercept is the y of the point where the line crosses the y-axis; that a line of best fit will hit or come close to most of the points; that the line of best fit can be used to predict other data points; that the equation of a line depends on the slope and the y-intercept.

Suggestions for Assessment

ASSESSMENT POINTS

Students write journal entries as described below:

- A. Summarize the experiment.
- **B.** What relationship did the centicubes have with the mass?
- **C.** What conclusions can be made about the number of raisins and their mass?
- **D.** What did the line of best fit (spaghetti) tell about this relationship?
- E. How would someone find the mass of 100 raisins?
- **F.** How would someone find out how many raisins weigh 200 grams?

Adaptations / Extensions

• Graph the following data using either paper and pencil or the graphing calculator.

| Number of Paper Clips | Weight |
|-----------------------|--------|
| 20 | 22 g |
| 30 | 30 g |
| 40 | 46 g |
| 50 | 54 g |
| 60 | 67 g |

- Sketch your graph on grid paper.
- Is there a linear relationship between the number of paper clips and the weight?
- Predict the weight of 35 paper clips.
- Predict the weight of 74 paper clips.
- More advanced classes could compute the line of best fit using the graphing calculator.
- The lesson referenced below uses a CBL and a force sensor to measure and form the lists for such an experiment. The lesson is very similar to the raisin activity and is lots of fun.

Activity 2, "Making Cents of Math" in *Real World Math with the CBL System* by Chris Brueninger, Bill Bower, Linda Antinone, Elisa Bruening, copyright 1994 by Texas Instruments.

Activity 1. Raisins: Collecting Data to Explore Mass Handout 2: Calculator Instructions

Give students copies of the appropriate version of Handout 2. Students will use the Calculator Instructions to find the answers to #17 - 20 in Handout 1.

Activity 2. Weight Through the Solar System Handout 1: Data Sheet

The math teacher may want to collaborate with the science teacher (if he/she does not teach science) for this activity.

Hopefully, your students will identify with, or at least readily recognize, the people you send through the solar system in the last activity. You may wish to choose important people in your school or community. We have included mostly athletes since their weights are readily available on the Internet (just search for a name you wish to include). Following is a sample list of people whose weights were found on the Internet.

Unofficial Celebrity Earth Weight List

| Lisa Leslie 165 pounds |
|------------------------------------|
| Rebecca Lobo 185 pounds |
| Brett Favre 225 pounds |
| John Stockton 175 pounds |
| Jackie Joyner-Kersee 154 pounds |
| Oprah Winfrey 150 pounds |
| Anfernee Penny Hardaway 210 Pounds |

The teacher may want to use Oprah's weight as an example and work through the Calculator Instructions as a teacher-led activity.

- Choose a celebrity from the list above.
 Answers will vary. For example: Oprah Winfrey
- On which planet would you expect the celebrity you chose to weigh the most?
 Jupiter, no matter which celebrity is chosen.
- 3. On which planet would you expect the celebrity you choose to weigh the least? **Pluto, no matter which celebrity is chosen.**

Sample Answers for Activity 2, Handout 1 (continued):

4. Calculate (calculator is optional) the values for the following table.

The following formula will be useful:

Planet Weight = Earth Weight * Planet's Gravitational Factor

(Gravitational factors are in comparison to the gravity on Earth; i.e., Earth = 1)

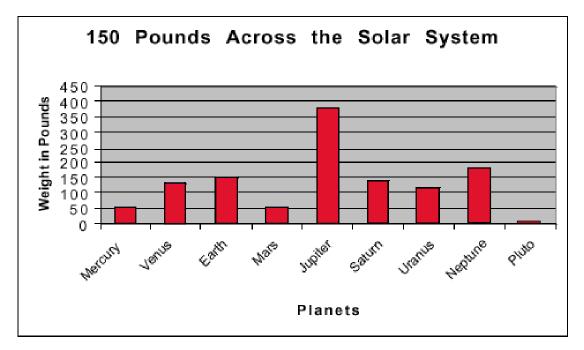
Answers will vary. For example, the numbers in the chart below are based on a weight on Earth for Oprah of 150 pounds and are rounded to one decimal place.

| Planets | Gravitational Factor* | Earth Weight * Gravitational Factor | Weight |
|---------|-----------------------|-------------------------------------|------------|
| Mercury | 0.38 | 150*.38 | 57 lbs. |
| Venus | 0.91 | 150*.91 | 136.5 lbs. |
| Earth | 1 | 150*1.0 | 150 lbs. |
| Mars | 0.38 | 150*.38 | 57 lbs. |
| Jupiter | 2.54 | 150*2.54 | 381 lbs. |
| Saturn | .93 | 150*.93 | 139.5 lbs. |
| Uranus | 0.8 | 150*.8 | 120 lbs. |
| Neptune | 1.2 | 150*1.2 | 180 lbs. |
| Pluto | 0.04 | 150*.04 | 6 lbs. |

*Different sources may give different values for gravitational factors: the ones in the table are approximate.

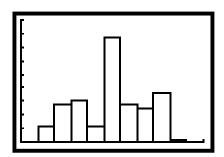
5. Create a bar graph using the results of the data showing the weight of the person on each planet.

Give the bar graph a title. Label the x-axis as the planets and the y-axis as the weight of the person. Choose an appropriate scale.



Sample Answers for Activity 2, Handout 1 (continued):

6. Use your graphing calculator and the Calculator Instructions in Handout 2 to make a bar graph on the calculator using the same data.



- 7. Which planet produced the highest weight? Jupiter
- 8. Which planet produced the lowest weight? Pluto
- 9. What was the range of the weights? Answers will vary.
- 10. What is the relationship between mass and weight? Weight is mass times the gravitational factor for each planet. Since Earth's factor is 1.0, the weight and mass are the same on Earth. Weight for the same mass varies as the gravitational factor varies.
- 11. What surprised you the most about the differences in the weights? Answers will vary. For example: the range was greater than I expected.
- 12. Name the planets that have similar gravitational pull. List the reason(s).

Mars and Mercury because they are somewhat the same size, although size is not the only factor. The Earth and Venus, which have similar gravitational pull, are similar in size, density, and somewhat the same distance from the sun.

13. Name three differences between the handmade bar graph and the calculator bar graph.

Answers will vary. Spaces between the bars on the handmade. Titles and axis labels on the handmade. The calculator is interactive by using the **TRACE** key.

- 14. Name three similarities in the process of making a handmade bar graph and the calculator bar graph. Each involves a chart or lists of data. An appropriate window or appropriate scales must be chosen for each axis.
- 15. Why would you want to know what you weigh on different planets? It would be important if you were going to travel to another planet.
- 16. Use your graphing calculator to find your own weight across the solar system and to make a bar graph showing the data. Record your data in the following chart and sketch the bar graph in the space below the chart. **Answers will vary per student.**

DISCUSSION POINTS

- What seems to be related to a person's weight on a planet? The size of the planet seems to be related. The distance from the sun seems unrelated.
 - If you know that Joe weighs 200 lbs. on Saturn, what does he weigh on Mercury?

$$\frac{200}{.93} = \frac{x}{.38}$$

Thus, Joe's weight on Mercury = 81.7 or 82 lbs.

• What is the relationship between mass and weight?

Answers will vary. For example: mass is always the same, whereas, weight depends on gravitational pull. You (your mass) would balance with the same number of, say, paper clips no matter where in space you go; but if you are weighed by a device that depends upon the pull of gravity, your weight will be different on different planets, etc.

• How does gravitational pull affect weight?

The greater the gravitational pull, the greater the weight.

• When are the mass and weight the same (if they ever are)?

As long as we remain on Earth, our weight and our mass are, for all practical purposes, the same. Of course our weight would be slightly different at different elevations.

- When you step on the scale, what are you measuring? Weight.
- If you could choose to live on any planet, which planet would you choose, now that you know your weight will change? Why?

Answers will vary. Those who want to weigh more will likely answer one of the planets larger than Earth. Those who want to weigh less will answer one of the planets smaller than Earth. Of course a person would look the same; it's just that the bathroom scales would read a different number.

Suggestion for Assessment

ASSESSMENT POINT

Given that the moon's gravitational pull is 1/6 that of the earth, have students find their chosen celebrity's weight on the moon.

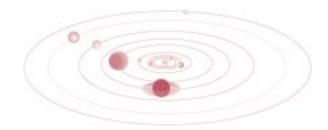
- —Is this comparable to any planet?
- -Who would use this information and why would they use it?

Adaptations / Extensions

On grid paper, make a scatterplot using the same data where the independent variable is the planets and the dependent variable is the weight. Give the scatterplot a title and label the axes. Discuss if the scatterplot or the bar graph gives a better picture of the data.

Activity 2. Weight Through the Solar System Handout 2: Calculator Instructions

- Give students the appropriate version of Handout 2 for the graphing calculator they are using.
- In the instructions, students will make a bar graph with the categories on the x-axis representing the nine planets and with the weights calculated for the various planets as the frequencies on the y-axis.



Lesson 16: Traveling Through the Solar System – Activity 1. Raisins: Collecting Data to Explore Mass – Handout 1: Data Sheet

1. Find the measures of the following using a balance scale. Place the given number of raisins on one side of the balance. Place centicubes (or other gram weights) on the other side of the balance until both sides are the same. The raisins weigh the number of centicubes. Remember, 1 centicube has a mass of 1 gram. Write the results in the table.

| Number of Raisins | Mass in grams |
|-------------------|---------------|
| 10 | |
| 20 | |
| 25 | |
| 30 | |
| 40 | |

- 2. What is the independent variable?
- 3. What is the dependent variable?
 - 4. Are these variables related? How?
 - 5. On the grid paper below, graph the number of raisins vs. the corresponding mass. Choose an appropriate scale.

| 4 | | | | | | | | | | | |
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Activity 1, Handout 1 (continued):

- 6. What relationship do these data points show?_____
- 7. Is there a positive relationship (that is, does the dependent variable increase/decrease when the independent variable increases/decreases), a negative relationship (that is, does the dependent variable increase/decrease when the independent variable decreases/increases), or no consistent relationship?
- 8. Even though the data points may not be in exactly one straight line, there may be a line that is close to most, if not all points. This is called the line of best fit. Use the spaghetti to find this line of best fit. Does the spaghetti intersect with every point, come close to most points, or not intersect any point?
- 9. What number value is the slope? To find the slope, choose any two of the data points that fall on or very close to the spaghetti and use the slope formula:

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

- 10. What does the slope represent in this problem?
- 11. According to the data, what should the y-intercept be?
- 12. What is the y-intercept according to the line of best fit (spaghetti)?_____
- 13. Is the value of #11 different from the value of #12? _____Why/Why not? ______
- 14. Write an equation for the line made by the spaghetti in the form y = mx + b where m is the slope and b is the y-intercept.

Data

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Activity 1, Handout 1 (continued):

15. Predict the missing values in the table by using the linear equation you found in #14.

| Number of Raisins | Mass in grams |
|-------------------|---------------|
| 10 | |
| 4 | |
| | 16 |
| | 95 |

- 16. Make a real-life graph. On a piece of heavier paper (construction paper, poster board), create an appropriate title for this graph. Draw axes for the first quadrant. Draw the hash marks along the axes and choose an appropriate scale. Glue the raisin pieces at the data points from #1. Glue on spaghetti as the line of best fit. Label the line of best fit with the equation from #14.
- 17. Use the graphing calculator and the Calculator Instructions in Handout 2 to find the value of the slope (a) and y-intercept (b). (Round to the hundredths place.)

Slope = _____

Y-intercept = _____

The equation for a line is y = mx + b (m = slope and b = y-intercept)

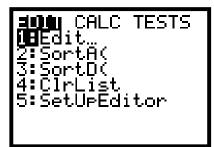
- 19. Sketch the graph of the line from your calculator screen.

- 20. How does the calculator slope and y-intercept compare with the slope and y-intercept from the spaghetti and pencil-and-paper calculations?
- 21. Name three new concepts that you learned from the experiment and/or three things that you now understand better because of the experiment.

Handout 1: Data Sheet ACTIVITY 1

Activity 1. Raisins: Collecting Data to Explore Mass Handout 2: TI-83 Plus Calculator Instructions

- 1. Clear any stat plots or equations that are in the calculator.
 - Press 2nd Y= (STATPLOT)
 - Press (4) (Plotsoff). This returns the cursor to the **Homescreen**.
 - Press **ENTER**. This will turn all of the stat plots off.
 - Press Y=. If any of the = signs are highlighted, move the cursor on top of the = and press ENTER. Doing this will make the graph of this equation invisible. If you do not want that equation anymore, keep the cursor on top of the equation and press CLEAR. Do one of these two things for any equation that is in any Y.
- 2. Enter the data into your calculator for the number of raisins that were weighed.
 - Press **STAT 1** (EDIT).
 - If the lists have data already entered in the columns, use the up arrow key to highlight L,.



| ন | L2 | L3 | 2 |
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| | | | _ |
| L1 = | | | |

- Press **CLEAR ENTER**. This should clear the data from that column. You may clear each of the columns this way.
- When the lists have been cleared, the data can be typed into the lists.
- If necessary, use arrow keys to move the cursor to the first place in L₁.

| L1 | L2 | L3 | 2 |
|---------|----|----|---|
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| L1(1) = | | | |

Plus

Handout 2: TI-83

TI-83 Plus Keystrokes (continued):

- Enter the number of raisins in L1 and the mass in grams in L2.
- After each entry, press **ENTER**.
- 3. Instruct the calculator to make the scatterplot (see the calculator screen that follows).
 - Press 2nd Y= (STATPLOT) and then ENTER with the cursor on Plot 1.
 Press ENTER while the cursor is flashing on top of the ON.
 - Press once. Move the cursor on top of the scatterplot, which is the first graph choice.
 Press ENTER to select this type of graph.
 - Arrow down once to Xlist. Press **2nd 1** (L_1) , **V 2nd 2** (L_2) .
 - Press 💌 and choose the type of mark you want to represent your data.



4. Set an appropriate window for viewing the scatterplot.

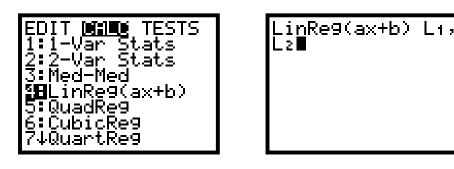
- Press WINDOW to set an appropriate window (see sample window settings that follow).
- Be sure to use numbers that include all data points. Buffer these points on all sides in order to see a complete graph.

| WINDOW Xmin=0 Xmax=50 Xscl=5 Ymin=-1 Ymax=20 Yscl=2 Xres=1 |
|---|
|---|

Press **GRAPH**. To look at the values of the points, press **TRACE**. A flashing cursor will appear on top of the first data point. At the bottom of the screen, X= and Y= will appear. To see the rest of the data points, press the key.

TI-83 Plus Keystrokes (continued):

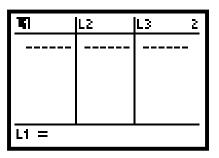
- 5. Find the slope and y-intercept for the line of best fit.
 - Press **STAT b** to CALC and press **4** for **LinReg**(ax + b).
 - Press **2nd 1** (L_1) , and **2nd 2** (L_2) .



- Press ENTER and record the values for *a* (slope) and *b* (y-intercept) on Handout 1, #17, to use as you complete Handout 1.
- 6. Graph the line of best fit and compare to the scatterplot.
 - To look at this graph, press Y=.
 - Type in the equation you wrote on Handout 1, #17. The window still contains the data points from above. Press GRAPH.
 - Sketch the graph on Handout 1, and then complete Handout 1.

Activity 1. Raisins: Collecting Data to Explore Mass -Handout 2: TI-73 Calculator Instructions

- 1. Clear any stat plots or equations that are in the calculator.
 - Press **2nd Y**= (PLOT)
 - Press (4) (Plotsoff). This returns the cursor to the **Homescreen**.
 - Press **ENTER**. This will turn all of the stat plots off.
 - Press Y=. If any of the = signs are highlighted, move the cursor on top of the = and press ENTER. Doing this will make the graph of this equation invisible. If you do not want that equation anymore, keep the cursor on top of the equation and press CLEAR. Do one of these two things for any equation that is in any Y.
- 2. Enter the data into your calculator for the number of raisins that were weighed.
 - Press LIST.
 - If the lists have data already entered in the columns, use the up arrow key to highlight L_1 .



- Press **CLEAR ENTER**. This should clear the data from that column. You may clear each of the columns this way.
- When the lists have been cleared, the data can be typed into the lists.
- If necessary use arrow keys to move the cursor to the first place in L₁.

| L1 | L2 | L3 | 2 |
|---------|----|----|---|
| | | | |
| | | | |
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| | | | |
| L1(1) = | | | |

- Enter the number of raisins in L1 and the mass in grams in L2.
- After each entry, press **ENTER**.

TI-73 Keystrokes (continued):

- 3. Instruct the calculator to make the scatterplot (see the calculator screen that follows).
 - Press 2nd Y= (PLOT) and then ENTER with the cursor on Plot 1. Press
 ENTER while the cursor is flashing on top of the ON.
 - Press
 once. Move the cursor on top of the scatter plot, which is the first graph choice.
 Press
 ENTER to select this type of graph.
 - Arrow down once to Xlist. Press **2nd LIST** (STAT) **1** (L_1) ,
 - **2nd LIST** (STAT) **2** (L_2) .
 - Press 💽 and select the type of mark you want to represent your data.



- 4. Set an appropriate window for viewing the scatterplot.
 - Press WINDOW to set an appropriate window (see sample window settings that follow).
 - Be sure to use numbers that include all data points (the calculator will set ΔX automatically). Buffer these points on all sides in order to see a complete graph.

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Press **GRAPH**. To look at the values of the points, press **TRACE**. A flashing cursor will appear on top of the first data point. At the bottom of the screen, X= and Y= will appear. To see the rest of the data points, press the key.

TI-73 Keystrokes (continued):

- 5. Find the slope and y-intercept for the line of best fit.
 - Press **2nd LIST** (STAT) and **\blacktriangleright** to **CALC** and press **5** for **LinReg(ax + b)**.
 - Press **2nd LIST** (STAT) **1** (L_1) , and **2nd LIST** (STAT) **2** (L_2) .

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- Press ENTER and record the values for *a* (slope) and *b* (y-intercept) on Handout 1, #17 to use as you complete Handout 1.
- 6. Graph the line of best fit and compare to the scatterplot.
 - To look at this graph, press **Y**=.

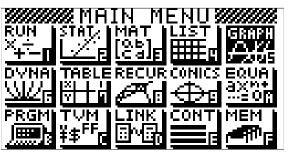
Handout 2: TI-7

- Type in the equation you wrote on Handout 1, #17. The window still contains the data points from above. Press **GRAPH**.
- Sketch the graph on Handout 1, and then complete Handout 1.

- Activity 1. Raisins: Collecting Data to Explore Mass -Handout 2: Casio CFX-9850GB Plus Calculator Instructions

- 1. Clear any equations that are in the calculator.
 - Beginning from the Main Menu, press 5. If any of the = signs are highlighted, move the cursor on top of the = and press F1. Doing this will make the graph of this equation

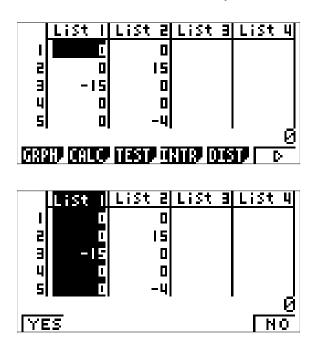
invisible. If you do not want that equation anymore, keep the cursor on top of the equation and press **F2 F1**. Do one of these two things for any equation that is in any **Y**.



- 2. Enter the data into your calculator for the number of raisins that were weighed.
 - Press MENU 2 to go to lists.

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|--------------|---|
| RUN | STATE MAT LIST GRAPH |
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| NVNA | TABLE RECUR CONICS FOUR |
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• If the lists have data already entered in the columns, press F6 F4 F1.



| Li 1 2 3 | St Li 0 -15 0 | i <u>st 2 L</u> 0 15 0 | ist 3 | List u | | |
|----------------|--------------------------|---------------------------------|-------|--------|--|--|
| 5 | | -4 | | g | | |
| SRTA | SRT-D D | EL DE | P IN: | | | |
| Li | St I Li | ist 2 L | ist 3 | List 4 | | |
| 2 | | 0 15 | | | | |
| 2 3 4 | | | | | | |
| 5 | | -4 | | | | |
| SRTA | SRTA SRTD DEL DEL DEL D | | | | | |

Handout 2: CFX-9850GB Plus ACTIVITY 1

- This should clear the data from that column. You may clear each of the columns by using the right arrow key to move to the desired list and pressing F4 F1.
- When the lists have been cleared, the data can be typed into the lists. If necessary use arrow keys to move the cursor to the first place in List 1.

| | List I | LiSt 2 | List B | LiSt | 4 |
|-----|---------|--------|--------|------|---|
| I | | | | | |
| 2 | | | | | |
| Е | | | | | |
| 5 | | | | | |
| | | | | | • |
| SRI | ra srto | DEL | EL PIN | SD | |

- Enter the number of raisins in List 1 and the mass in grams in List 2. After each entry, press
 EXE.
- 3. Instruct the calculator to make the scatterplot (see the calculator screen that follows).
 - Press F6 F1 F6. Use the arrow key to move to Graph Type and choose Scat. Set the window as below, setting Xlist to List1, Ylist to List2, and selecting a Mark Type to represent your data. Press EXE to return to lists.

| StatGraph1 | |
|-------------|------------|
| Graph Type | :Scatter |
| XList | :List1 |
| YList | :List2 |
| Frequency | : <u>1</u> |
| Mark Type | |
| Graph Color | :Green |
| Scat XY NPP | D |

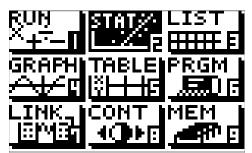
- 4. To set an appropriate window, press **SHIFT MENU** (SET UP), set **Stat Wind** to **Auto**, and turn **Coord** to **On**.
 - Press EXE to return to lists, *or* set Stat Wind to Man and turn Coord to On. Press
 EXE SHIFT F3 and set an appropriate window. Be sure to use numbers that include all data points. Buffer these points on all sides in order to see a complete graph.
 - Store these settings by pressing **F4 STO F1**. Press **EXE EXIT** to return to lists and original list menu.
 - Press F1 F4 and turn StatGraph1 On and the others Off. Press F6 to draw the graph. To look at the values of the points, press SHIFT F1 (Trace). A flashing cursor will appear on top of the first data point, and the (x,y) coordinates will appear at the bottom of the screen. To see the rest of the data points, press the key.
- 5. Find the slope and y-intercept for the line of best fit. Press **F1** for **LinearReg**(y=ax+b) and record the values for *a* (slope) and *b* (y-intercept) on Handout 1, #17, to use as you complete Handout 1.
- 6. Graph the line of best fit and compare to the scatterplot. To look at this graph, press **F6**.
 - Sketch the graph on Handout 1, and then complete Handout 1.

Activity 1. Raisins: Collecting Data to Explore Mass Handout 2: Casio FX-7400GB Plus Calculator Instructions

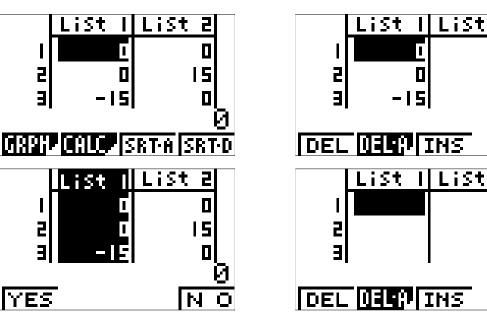
- 1. Clear any equations that are in the calculator.
 - Beginning from the Main Menu, press 4. If any of the = signs are highlighted, move the cursor on top of the = and press F1. Doing this will make the graph of this equation invisible. If you do not want that equation anymore, keep the cursor on top of the equation and press F2 F1. Do one of these two things for any equation that is in any Y.



- 2. Enter the data into your calculator for the number of raisins that were weighed.
 - Press **MENU 2** to go to lists.



• If the lists have data already entered in the columns, press F F



andout 2: FX-7400G

(F1).

2

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2

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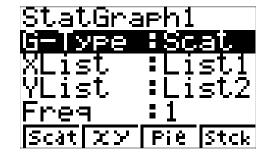
5

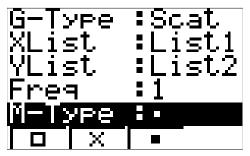
Π

- This should clear the data from that column. You may clear each of the columns by using the right arrow key to move to the desired list and
 - pressing **F2 F1**.
- When the lists have been cleared, the data can be typed into the lists. If necessary use arrow keys to move the cursor to the first place in List 1.
- Enter the number of raisins in List 1 and the mass in grams in List 2. After each entry, press EXE.



- 3. Instruct the calculator to make the scatterplot (see the calculator screen that follows).
 - Press F> F1 F> F4. Use the arrow key to move to G-Type and choose Scat. Set the window as below, setting Xlist to List1, Ylist to List2, and selecting an M-Type to represent your data. Press EXE to return to lists.





- 4. To set an appropriate window, press **SHIFT MENU** (SET UP) and set **S-Wind** to **Auto**, or set **S-Wind** to **Man**.
 - Press EXE SHIFT F3 to set an appropriate window. Be sure to use numbers that include all data points. Buffer these points on all sides in order to see a complete graph. Store these settings by pressing F3 (Sto). Press EXE QUIT to return to lists and original list menu.
 - Press **F1 F F1** and turn **S-Grph1 On** and the others **Off.**
 - Press **F4** to draw the graph.
 - To look at the values of the points, press SHIFT F1 (Trace). A flashing cursor will appear on top of the first data point, and the (x,y) coordinates will appear at the bottom of the screen. To see the rest of the data points, press the key.
 - Find the slope and y-intercept for the line of best fit.
- 5. Press **F1** for LinearReg y=ax+b and record the values for *a* (slope) and *b* (y-intercept) on Handout 1, #17, to use as you complete Handout 1.
- 6. Graph the line of best fit and compare to the scatterplot. To look at this graph, press **F4**.
 - Sketch the graph on Handout 1, and then complete Handout 1.

Activity 2. Weight Through the Solar System -Handout 1: Data Sheet

Unofficial Celebrity Earth Weight List

| 165 pounds |
|------------|
| 185 pounds |
| 225 pounds |
| 175 pounds |
| 154 pounds |
| 150 pounds |
| 210 Pounds |
| |

- 1. Choose a celebrity from the list above.
- 2. On which planet would you expect the celebrity you chose to weigh the most?
- 3. On which planet would you expect the celebrity you choose to weigh the least?
- 4. Calculate (calculator is optional) the values for the following table. The following formula will be useful: Planet Weight = Earth Weight * Planet's Gravitational Factor (Gravitational factors are in comparison to the gravity on Earth; i.e., Earth = 1)

| Planets | Gravitational Factor* | Earth Weight *Gravitational Factor | Weight |
|---------|-----------------------|------------------------------------|--------|
| Mercury | 0.38 | | |
| Venus | 0.91 | | |
| Earth | 1 | | |
| Mars | 0.38 | | |
| Jupiter | 2.54 | | |
| Saturn | .93 | | |
| Uranus | 0.8 | | |
| Neptune | 1.2 | | |
| Pluto | 0.04 | | |

*Different sources may give different values for gravitational factors: the ones in the table are approximate.

Activity 2, Handout 1 (continued):

5. Create a bar graph using the results of the data showing the weight of the person on each planet.

Give the bar graph a title. Label the x-axis as the planets and the y-axis as the weight of the person. Choose an appropriate scale.

6. Use your graphing calculator and the Calculator Instructions in Handout 2 to make a bar graph on the calculator using the same data.

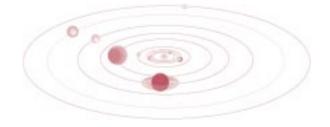
Activity 2, Handout 1 (continued):

- 7. Which planet produced the highest weight?
- 8. Which planet produced the lowest weight?
- 9. What was the range of the weights?
- 10. What is the relationship between mass and weight?
- 11. What surprised you the most about the differences in the weights?
- 12. Name the planets that have similar gravitational pull. List the reason(s).
- 13. Name three differences between the handmade bar graph and the calculator bar graph.
- 14. Name three similarities in the process of making a handmade bar graph and the calculator bar graph.
- 15. Why would you want to know what you weigh on different planets?

Activity 2, Handout 1 (continued):

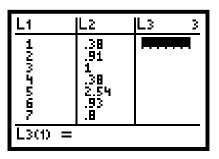
16. Use your graphing calculator to find your own weight across the solar system and to make a bar graph showing the data. Record your data in the following chart and sketch the bar graph in the space below the chart.

| Planets | Gravitational Factor* | Earth Weight *Gravitational Factor | Weight |
|---------|-----------------------|------------------------------------|--------|
| Mercury | 0.38 | | |
| Venus | 0.91 | | |
| Earth | 1 | | |
| Mars | 0.38 | | |
| Jupiter | 2.54 | | |
| Saturn | .93 | | |
| Uranus | 0.8 | | |
| Neptune | 1.2 | | |
| Pluto | 0.04 | | |

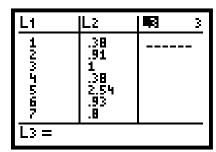


Activity 2. Weight Through the Solar System Handout 2: TI-83 Plus Calculator Instructions

- 1. Number the planets in L1 and enter the gravitational factors in L2.
 - Press STAT 1 (EDIT). If the lists have data already entered in the columns, use the up arrow key to highlight L₁.
 - Press **CLEAR ENTER**. This should clear the data from that column. You may clear each of the columns this way.
 - Move the cursor to highlight the first entry under L_1 .
 - Press 1 ENTER, 2 ENTER, 3 ENTER, etc., until you have entered the numbers 1 through 9, which would represent the nine planets.
 - **(b)** to move to the first entry under L₂. Enter the gravitational factors for each planet from Handout 1.



- 2. Give the calculator instructions to calculate the weights of your celebrity on each of the nine planets.
 - Move your cursor up to highlight L3.
 - Press ALPHA + ("). Then enter the Earth weight of your celebrity in pounds (the example below is for Oprah).
 - Press X and 2nd 2 (L2) to multiply the weight by the gravitational factors in L2.
 - Press **ALPHA** + ("), and press **ENTER**.

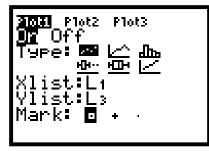


| <u>L1</u> | L2 | R 3 | | | | |
|---------------|--|------------|--|--|--|--|
| 12075007 | 81 81 85 1 85 1 85 1 85 1 85 1 85 1 85 | | | | | |
| L3 = "150*L2" | | | | | | |

| L1 | L2 | L3 • 3 | 3 | | | |
|----------|---|---|---|--|--|--|
| нимания | .38 .91 .384 .254 .93 .8 | 136.5 150 57 381 139.5 120 | | | | |
| L300 =57 | | | | | | |

TI-83 Plus Keystrokes (continued):

- 3. Give the calculator instructions for making a bar graph using L1 (planet numbers) for Xlist and L3 (weights across the planets) for Freq.
 - Press Y = and clear any Y = that is not clear.
 - Press **2nd Y** = (STAT PLOT), **ENTER ENTER** to turn on **Plot 1.**
 - **v** to **Type**, **b** until the 3rd graph is highlighted and press **ENTER**.
 - \checkmark to Xlist: and press **2nd 1** (L₁), \checkmark to Freq: and press **2nd 3** (L₃).



4. Set an appropriate window to view the bar graph.

Press WINDOW. Be sure to use numbers that include all of the data points. Buffer these points on all sides in order to see the complete graph (sample window is shown below).

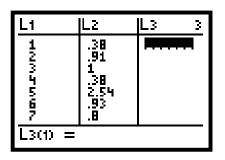
| WINDOW Xmin=0 Xmax=11 Xscl=1 Ymin=0 Ymax=450 | |
|---|--|
| Ymax=450 Yscl=50 Xres=1 | |

- The Xlist is the horizontal axis, which will be the planets. The Freq (frequency) is the vertical axis, which will represent the weight of the person on the given planet.
- 5. View the graph by pressing **GRAPH**.
 - To look at specific values of the bars, press **TRACE**. Use the right arrow key to move the cursor to the top of the first bar, which is Mercury. At the bottom right of the screen, there is an n=. This is the weight value for the planet. Press the right arrow key. The flashing cursor will jump to the top of the other bars. Look at the n= for the weight value.
- 6. To put in your weight or that of another celebrity, press STAT 1 (EDIT) and arrow up to L3 and press ENTER. Change the Earth weight number to the new Earth weight and press ENTER. L3 will now contain the weights across the planets for the new Earth weight.

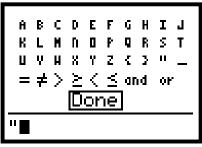
Handout 2: TI-83 Plus

Activity 2. Weight Through the Solar System – Handout 2: TI-73 Calculator Instructions

- 1. Number the planets in L1 and enter the gravitational factors in L2.
 - Press LIST. If the lists have data already entered in the columns, use the up arrow key to highlight L₁.
 - Press **CLEAR ENTER**. This should clear the data from that column. You may clear each of the columns this way.
 - Move the cursor to highlight the first entry under L_1 .
 - Press 1 ENTER, 2 ENTER, 3 ENTER, etc., until you have entered the numbers 1 through 9 which would represent the nine planets.
 - **(b)** to move to the first entry under L₂. Enter the gravitational factors for each planet from Handout 1.

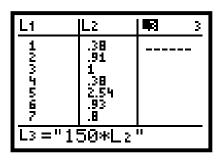


- 2. Give the calculator instructions to calculate the weights of your celebrity on each of the nine planets.
 - Move your cursor up to highlight L3.
 - Press 2nd MATH (TEXT). Capture the quotation mark (") and then capture DONE.



TI-73 Plus Keystrokes (continued):

- Press ENTER. Then enter the Earth weight of your celebrity in pounds (the example below is 150 lbs. for Oprah).
- Press X and 2nd LIST (STAT) 2 (L2) to multiply the weight by the gravitational factors in L2.
- Press 2nd MATH (TEXT). Capture the quotation mark ("), press ENTER, then capture DONE and press ENTER.

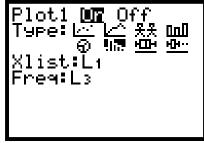


| Ĥ | B | с | D | E | F | G | H | I | L |
|---|---|---|--------|-----------|--------|----|----|----|---|
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| Ш | Ŷ | H | Х | Y | Z | £ | 3 | П | _ |
| = | ŧ | > | \geq | \langle | \leq | ar | ıd | ٥٢ | - |
| | - | - | D | or | ìe |] | | | |
| " | | | | | | | | | |

 Press ENTER again to see the weights across the planets (the example below shows Oprah's weights across the planets.)

| L1 | Lz | L3 🔹 3 | | |
|-----------|---|---|--|--|
| HNMJWOR | .91 195 1,85 1,85 1,85 1,85 1,85 1,85 1,85 1,8 | 57 136.5 150 57 381 139.5 120 | | |
| L3(1) =57 | | | | |

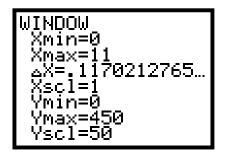
- 3. Give the calculator instructions for making a histograph using L1 (planet numbers) for Xlist and L3 (weights across the planets) for Freq.
 - Press Y = and clear any Y = that is not clear.
 - Press **2nd Y** = (PLOT), **ENTER ENTER** to turn on **Plot 1.**
 - **v** to **Type**, **b** until the **6th graph** is highlighted and press **ENTER**.
 - ▼ to Xlist: and press 2nd LIST (STAT) 1 (L₁), ▼ to Freq: and press 2nd LIST 3 (STAT) (L₃).



Handout 2: TI-73 ACTIVITY 2

TI-73 Plus Keystrokes (continued):

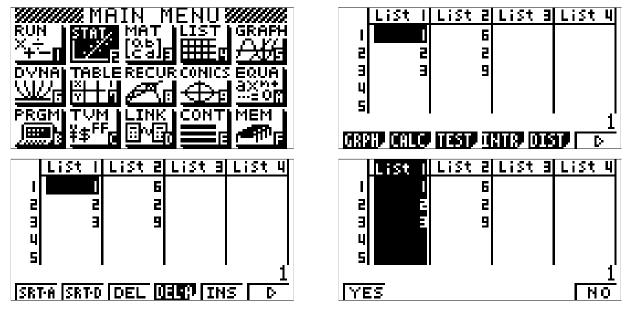
- 4. Set an appropriate window to view the bar graph.
 - Press **WINDOW**. Be sure to use numbers that include all of the data points. Buffer these points on all sides in order to see the complete graph (sample window is shown below).



- The **Xlist** is the horizontal axis, which will be the planets. The **Freq** (frequency) is the vertical axis, which will represent the weight of the person on the given planet.
- 5. View the graph by pressing **GRAPH**.
 - To look at specific values of the bars, press **TRACE**. Use the right arrow key to move the cursor to the top of the first bar, which is Mercury. At the bottom right of the screen, you'll see an **n**=. This is the weight value for the planet. Press the right arrow key. The flashing cursor will jump to the top of the other bars. Look at the **n**= for the weight value.
- 6. To put in your weight or that of another celebrity, press LIST and arrow up to L3 and press ENTER. Change the Earth weight number to the new Earth weight and press ENTER.
 L3 will now contain the weights across the planets for the new Earth weight.

— Activity 2. Weight Through the Solar System — Handout 2: Casio CFX-9850GB Plus Calculator Instructions

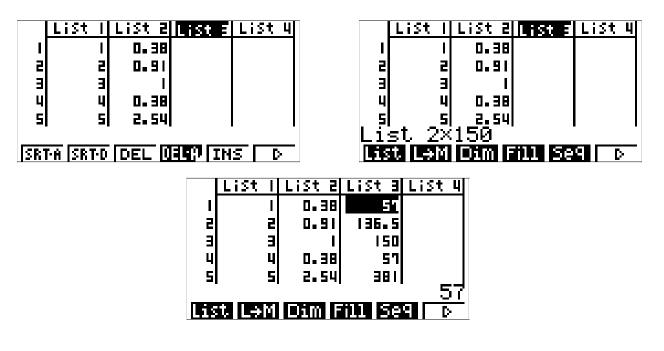
- 1. Number the planets in List 1 and enter the gravitational factors in List 2.
 - From the Main Menu press 2. If the lists have data already entered in the columns, press
 F6 F4 F1. This should clear the data from that column.



- Use the arrow key to move to another list and press **F4 F1** to clear.
- When the columns are clear, move the cursor to highlight the first entry under List 1.
- Press 1 EXE 2 EXE 3 EXE, etc., until you have entered the numbers 1 through 9, which would represent the nine planets.
- **(b)** to move to the first entry under **List 2.** Enter the gravitational factors for each planet from Handout 1.



- 2. Give the calculator instructions to calculate the weights of your celebrity on each of the nine planets.
 - Move your cursor up to highlight **List 3.**
 - Press OPTN F1 F1 2 X, then enter the Earth weight of your celebrity in pounds (the example below is for Oprah). Press EXE.



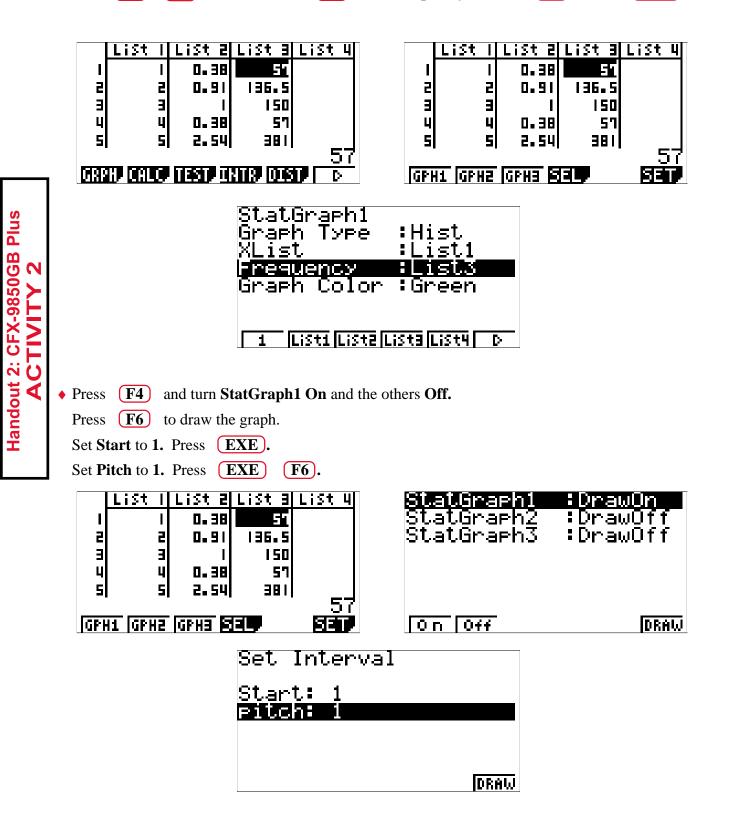
- 3. Give the calculator instructions for making a bar graph using List 1 (planet numbers) for Xlist and List 3 (weights across the planets) for Freq.
 - Press **SHIFT MENU** and set **Stat Wind** to **Auto**.

Handout

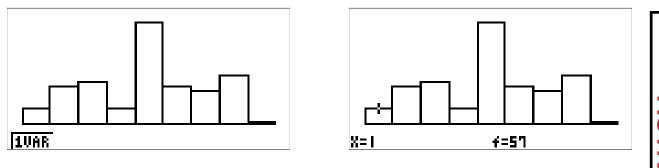
CFX-9850GB

Plus

♦ Press EXE to return to lists. Press EXIT EXIT F1 F6. Set the Graph Type to Hist (F6 F1), Xlist to List1 (F1), and Frequency to List3 (F4). Press EXE.



- 4. To view the graph, follow the instructions below.
 - The **Xlist** is the horizontal axis, which will be the planets. The **Freq** (frequency) is the vertical axis, which will represent the weight of the person on the given planet.
 - View the graph by pressing **F6**.
 - To look at specific values of the bars, press SHIFT F1. Use the right arrow key to move the cursor to the top of the first bar, which is Mercury. At the bottom right of the screen, you'll see an f=. This is the weight value for the planet. Press the right arrow key. The flashing cursor will jump to the top of the other bars. Look at the f= for the weight value.

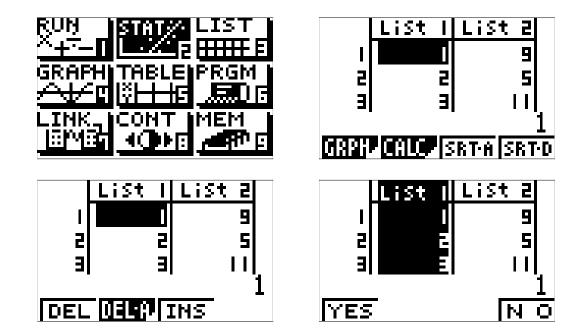


- 5. To put in your weight or that of another celebrity, press **EXIT EXIT** and move the cursor to the top of **List 3.** Press **OPTN F1 F1 2 X**, then enter the Earth weight in pounds.
 - Press EXE. List 3 will now contain the weights across the planets for the new Earth weight.

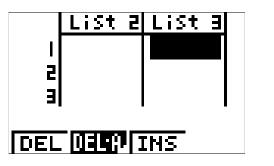
| | LiSt I | LiSt 2 | List 3 | LiSt 4 | | |
|---------------------------|--------------|--------|--------|--------|--|--|
| I | I | 0.38 | 57 | | | |
| 2 | 2 | 0.91 | 136.5 | | | |
| Ξ | 3 | I | 150 | | | |
| 4 | Ц | 0.38 | 57 | | | |
| 5 | 5 | 2.54 | 381 | | | |
| L1: | <u>st 2×</u> | | | | | |
| List LaM Dim Fill Seq 🕞 🛛 | | | | | | |

— Activity 2. Weight Through the Solar System — Handout 2: Casio FX-7400G Plus Calculator Instructions

- 1. Number the planets in List 1 and enter the gravitational factors in List 2.
 - From the Main Menu press 2. If the lists have data already entered in the columns, press
 F F2 F1. This should clear the data from that column.



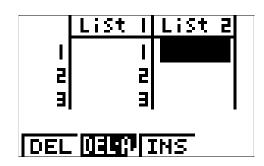
- Use the right arrow key to move to another list and press **F4 F1** to clear.
- When the columns are clear, move the cursor to highlight the first entry under List 1.

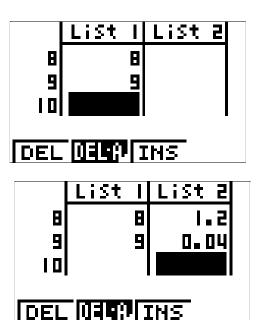




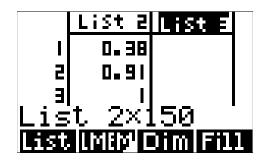
436 Lesson 16

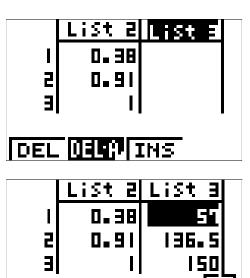
- Press 1 EXE, 2 EXE, 3
 EXE, etc., until you have entered the numbers 1 through 9 which would represent the nine planets.
- **b** to move to the first entry under **List 2.** Enter the gravitational factors for each planet from Handout 1.





- 2. Give the calculator instructions to calculate the weights of your celebrity on each of the nine planets.
 - Move your cursor up to highlight List 3.
 - Press OPTN F1 F1 2 X, then enter the Earth weight of your celebrity in pounds (the example below is for Oprah). Press EXE.



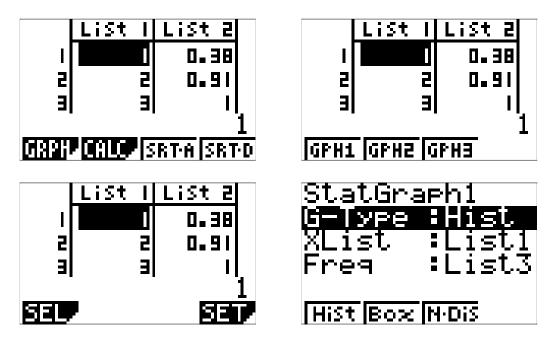


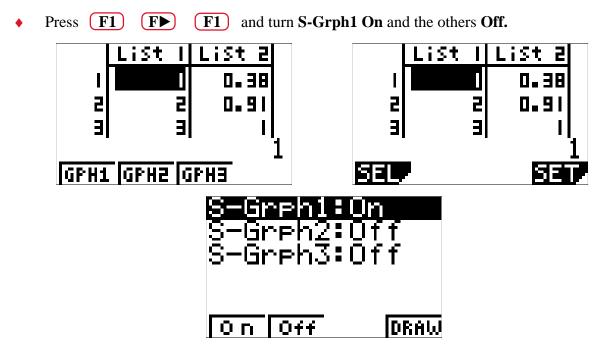
List LMEM Dim

- 3. Give the calculator instructions for making a bar graph using List 1 (planet numbers) for **Xlist** and **List 3** (weights across the planets) for **Freq.**
 - Press **SHIFT MENU** and set **S-Wind** to **Auto**.

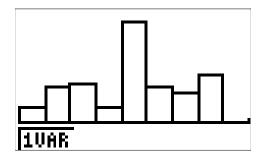


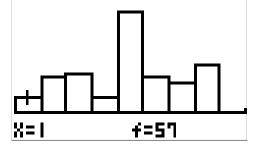
♦ Press EXE to return to lists. Press QUIT F1 F▶ F4. Set G-Type to Hist by pressing F▶ F1, Xlist to List1, and Frequency to List3. Press EXE.





- 4. View the graph by pressing **F4**. The **Xlist** is the horizontal axis, which will be the planets. The **Freq** is the vertical axis, which will be the weight of the person on the given planet.
 - To look at specific values of the bars, press SHIFT F1. Use the right arrow key to move the cursor to the top of the first bar, which is Mercury. At the bottom right of the screen, you'll see an f=. This is the weight value for the planet. Press the right arrow key. The flashing cursor will jump to the top of the other bars. Look at the f= for the weight value.





5. To put in your weight or another celebrity, press QUIT and move the cursor to the top of List 3. Press OPTN F1 F1 2 X, then enter the Earth weight in pounds. Press EXE. List 3 will now contain the weights across the planets for the new Earth weight.

